

Quadratic functions Solutions

Q1. $y = (x-1)^2 - 16$

(a) TP = (1, -16)

(b) $x = 1$

(c) A and B are the roots $\Rightarrow y = 0$

$$\begin{aligned} (x-1)^2 - 16 &= 0 \\ (x-1)(x-1) - 16 &= 0 \\ x^2 - x - x + 1 - 16 &= 0 \\ x^2 - 2x - 15 &= 0 \\ (x+3)(x-5) &= 0 \\ x+3=0 &\quad x-5=0 \\ x=-3 &\quad x=5 \\ A(-3,0) &\quad B(5,0) \end{aligned}$$

Q2. $7 + 6x - x^2 = 0$
 $(7 - x)(1 + x) = 0$
 $7-x=0 \quad 1+x=0$
 $\underline{7=x} \quad \underline{x=-1}$

TP: x -coordinate lies half-way between -1 and 7
 $\therefore x = 3$

Sub. 3 in for x

$$\begin{aligned} y &= 7 + 6x - x^2 \\ y &= 7 + 6(3) - (3)^2 \\ y &= 7 + 18 - 9 \\ y &= 16 \end{aligned}$$

TP = (3, 16)

Q3. $y = (x+2)^2 - 16$

(a) P = (-2, -16)

(b) $-2 \rightarrow 2 = 4$ units
 $2+4=6$

Q = (6, -16)

(c) $6+4+4=14$
 $S = (14, -16)$

$$\begin{aligned} y &= (x-a)^2 + b \\ y &= (x-14)^2 - 16 \end{aligned}$$

Q4. $y = 36 - (x-2)^2$

(a) TP = (2, 36)

(b) $x = 2$

Q5 (c) $y = 20 \quad y = 36 - (x-2)^2$

Sub. 20 instead of 36

axis of symmetry $\rightarrow x=2$

$$\begin{aligned} 20 &= 36 - (x-2)^2 \\ 20-36 &= -(x-2)^2 \\ -16 &= -(x-2)^2 \\ 16 &= (x-2)^2 \\ 4 &= |x-2| \end{aligned}$$

$S = (-2, 20)$

Q5. (a) $y = (x-3)^2 - 4$
 $TP = (3, -4)$

(b) $x = 3$

(c) A(1, 0) \downarrow axis (half-way)
 $1 \rightarrow 3 = 2$ units
 $3+2=5 \quad B(5,0)$

Q6. (a) $V = L \times B \times H$

$$\begin{aligned} V &= x(x+5)(1) = x^2 + 5x = 24 \\ x^2 + 5x - 24 &= 0 \end{aligned}$$

(b) $x^2 + 5x - 24 = 0$

$$(x-3)(x+8) = 0$$

$$x-3=0 \quad x+8=0$$

$$x=3 \quad x \neq -8$$

length can't be negative

breadth = $x = 3$

Q7. (a) $8x - x^2 = 0$

$$x(8-x) = 0$$

$$\underline{x=0} \quad \text{or} \quad \underline{8-x=0}$$

$$x=8$$

(b) axis lies half-way between roots
 $\Rightarrow x = 4$

(c) TP \Rightarrow sub 4 for x into $y = 8x - x^2$
 $y = 8(4) - 4^2 = 32 - 16 = 16$

TP = (4, 16)

Q8. (a) $f(a, b)$ = turning point

$$a = -5 \quad b = 1$$

(b) $x = -5$

(c) P \Rightarrow y-intercept $x=0$

$$y = (0 - 5)^2 + 1$$

$$y = 25 + 1$$

$$y = 26 \quad P(0, 26)$$

Q has same y-coordinate
as axis of symmetry

$$0 \rightarrow 5 = 5 \text{ units}$$

$$5 + 5 = 10$$

$$\Rightarrow Q = (10, 26)$$