## National 5 Revision Questions

## Q1. Calculate the area of PQR



Q2. A line passes through $(-2,3)$ and $(3,-5)$. State the equation of the line.

Q3. Calculate the length of PR


Q5. Calculate the area of the rectangle, give your answer as a surd in its simplest form.

Q4.

Find the equation of the line through the point $(-1,4)$ which is parallel to the line with equation $3 x-y+2=0$.

Q6.

A function $f$ is given by $f(x)=2 x^{2}-x-9$.
Which of the following describes the nature of the roots of $f(x)=0$ ?
A No real roots
B Equal roots
C Real distinct roots
D Rational distinct roots

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Q7.

In the diagram below the volume of the cylinder is double that of the cube


Calculate the height of the cylinder.

Q9.
Calculate the area of the triangle, give your answer as a surd in its simplest form.


Q11.

The stem and leaf diagram shows the cost of cars in a show room.

| 10 | 4 | 5 | 5 | 7 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 11 | 2 | 3 | 6 |  |  |  |
| 12 | 0 | 1 | 5 | 5 | 5 | 7 |
| 13 | 1 | 8 | 9 |  |  |  |

(a) Find the range of the costs
(b) Find the median cost.

Q8.

Find the range of values of $k$ such that the equation $k x^{2}-x-1=0$ has no real roots.

Q10.
Here are two statements about the roots of the equation $x^{2}+x+1=0$ :
(1) the roots are equal;
(2) the roots are real.

Which of the following is true?
A Neither statement is correct.
B Only statement (1) is correct.
C Only statement (2) is correct.
D Both statements are correct.

Q12.
In the diagram RSTU, VWXY represents a cuboid.
$\overrightarrow{\text { SR }}$ represents vector $f, \overrightarrow{\text { ST }}$ represents vector $g$ and $\overrightarrow{S W}$ represents vector $h$. Express $\overrightarrow{\text { VT }}$ in terms of $f, \boldsymbol{g}$ and $\boldsymbol{h}$.


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Q13.
The number goals scored by 20 football teams on Saturday were

(a) What is the modal number of goals scored?
(b) Find the median.

## Q15. Calculate the total volume



Q17. Simplify


Q14. The equation $3 x^{2}+x+m=0$ has equal roots. What is the value of $m$ ?

Q16. $7-8 x-x^{2}$ is expressed in the form $a-(x+b)^{2}$. What is the value of $a$ ?

Q18. Here are two statements about the roots of equation
$x^{2}-x-2=0$
(1) The roots are rational
(2) The roots are real

Which of the following is true?
A Neither statement is correct.
B Only statement 1 is correct.
C Only statement 2 is correct.
D Both statments are correct.

## National 5 Revision Questions

## Q19.

The cost of a holiday increased by $8 \%$ from the years 2001 to 2002 . If it cost $£ 540$ for the holiday in 2002, what was the cost in 2001 ?

## Q21. Find the value of

$$
25^{\frac{3}{2}}
$$

Q23.

The marks of 7 pupils in an advanced higher maths exam were

$$
\begin{array}{lllllll}
77 & 67 & 43 & 90 & 66 & 93 & 75
\end{array}
$$

Calculate the mean and standard deviation of these marks.

## In the diagram, ABCD represents a tetrahedron. A

Q20.
$B C$ represents $p, \overrightarrow{C D}$ represents $q$,
$\overrightarrow{D B}$ represents $\mathrm{r}, \overrightarrow{B A}$ represents s ,
$\overrightarrow{C A}$ represents t and $\overrightarrow{D A}$ represents u .
One of the statements is false, which one?


A $p=-q+s-u$
B $q=-p+s+u$
C $r=-p-t+u$
D $s=p+q+u$

Q22. A line through the points $A(2 k, 3)$ and $B(k, 5)$ has a gradient of 4 . What is the value of $k$ ?

Q24. $(x+4)(x-2)$ can be written in the form $(x+a)^{2}+b$. What is the value of $b$ ?

## Q25.

The large Magellanic cloud is $1.69 \times 10^{18}$ kilometres from Earth. Write this distance as an ordinary number

Q26. Solve

$$
\frac{x(x+5)}{4}=9
$$

Q28.
$\left(t^{4}\right)^{3}$

Q30. Find the diagonal $A C$


## National 5 Revision Questions

Q31.
The following rectangles have the same area. Find the value of x .


Q33.

The following diagrams show a triangle ABC

(a) Calculate the length of AB (to 2 significant figures). Do not use a scale drawing.
(b) Calculate the area of triangle ABC

Q32.
Write the vector AM in terms of $r$ and $q$


Write the vector AD in terms of $a$ and $b$ Q34.


Write the vector AC in terms of $a$ and $b$ Q36.


## National 5 Revision Questions

Q37.

Evaluate

$$
3 \frac{2}{5}-1 \frac{3}{4}
$$

Q3


Find the equation of this straight line in the form $y=m x+c$

Write the vector $B C$ in terms of $s$ and $t$ Q38.


Write the vector EC in terms of $s$ and $t$ Q40.


Q42.
Find the diagonal AC


## National 5 Revision Questions

Q43.

$$
t^{11 \div} \div 5
$$

Q44. Find the height


Q45.


Q47. Simplify

$$
\left(3 x^{2} y\right)^{2}
$$

Q48. Multiply out and simplify

$$
(1+\sqrt{2})^{2}
$$

## National 5 Revision Questions

Q49.

$$
\frac{6 y^{5} \times 2 y^{6}}{4 y^{8}}
$$

Q50.

$$
\frac{8 y^{9}}{2 \mathrm{y} \times 2 \mathrm{y}^{3}}
$$

Q51.
Solve

$$
4 x-5>2 x-15
$$

Q53.

$$
P=R^{3} b-5
$$

Change the subject of the formula to $R$.

Q54.
$\sqrt{75}-\sqrt{48}$

## National 5 Revision Questions

Q55.

Two vectors are defined as $\boldsymbol{u}=\binom{2}{-5}$ and $\boldsymbol{v}=\binom{-4}{3}$.
(a) Find the resultant vector $\boldsymbol{u}+3 \boldsymbol{v}$.
(b) Find $|\boldsymbol{u}+3 \boldsymbol{v}|$.

Q57.

Find the point of intersection of the straight lines with equations $2 x+y=5$ and $x-3 y=6$.

Q56.


Part of the graph of $y=\cos b x^{\circ}$ is shown in the diagram.
State the value of $b$.

Q58.

A parabola has equation $y=x^{2}-3 x+7$.
Using the discriminant, determine the nature of its roots.

Q59.


The equation of the parabola in the diagram above is $y=(x-2)^{2}-9$.
(a) State the coordinates of the minimum turning point of the parabola
(b) Find the coordinates of C
(c) A is the point $(-1,0)$. State the coordinates of B .

Q60.

Express $\frac{3}{x}-\frac{5}{x+2}, x \neq 0, x \neq 2$, as a single fraction in its simplest form.

Q61.

The total emissions of greenhouse gases by the USA in 2007 amounted to the equivalent of 7.2 million tonnes of carbon dioxide. If the annual increase in emissions is $1.2 \%$, calculate the total amount of emissions of greenhouse gases by the USA expected in 2010. Give your answer in millions of tonnes to 2 s.f.

## Q62. Multiply out and simplify

$$
(3 x-1)\left(2 x^{2}+3 x-4\right)
$$

Q64.
The diagram below shows the graph of $y=a x^{2}$.


Find the value of $a$.

150 patients have been given a flu vaccine.
The data is shown in the table below.
Q66.

| AGE | GENDER |  |
| :---: | :---: | :---: |
|  | male | female |
| 5 or under | 4 | 3 |
| $6-15$ | 7 | 8 |
| $16-59$ | 37 | 47 |
| 60 or over | 12 | 32 |

What is the probability that
(a) a patient given the flu vaccine was male and aged 60 or over?
(b) a patient given the flu vaccine was aged 5 or under?

## National 5 Revision Questions

Q67.
Joan buys gold and silver charms to make bracelets.
2 gold charms and 5 silver charms cost $£ 125$
(a) Let $g$ pounds be the cost of one gold charm and $s$ pounds be the cost of one silver charm.
Write down an equation in terms of $g$ and $s$ to illustrate the above information.

4 gold charms and 3 silver charms cost $£ 145$
(b) Write down another equation in terms of $g$ and $s$ to illustrate this information.
(c) Hence calculate the cost of each type of charm.

Q69. The parabola with equation $y=x^{2}-2 x-3$ cuts the $x$-axis at the points A and B as shown in the diagram.

(a) Find the coordinates of A and B.
(b) Write down the equation of the axis of symmetry of $y=x^{2}-2 x-3$.

Q71.


## Q68.

Solve the inequality

$$
4 x-5 \leq 7 x-20
$$

Q70.

Solve the equation

$$
2 x^{2}+7 x-3=0
$$

Give your answers correct to 1 decimal place.

Q72 A mobile phone mast, $18 \cdot 2$ metres high, stands vertically in the centre of a circle.
It is supported by a wire rope, 19 metres long, attached to the ground at a point on the circumference of the circle, as shown.


Calculate the circumference of the circle.

Q73.
As the pendulum of a clock swings, its tip moves through an arc of a circle.


The length of the pendulum is 50 centimetres The length of the arc is 36.7 centimetres. Calculate $x^{\circ}$, the angle through which the pendulum swings.

Q75.
(a) Express $\frac{a^{\frac{1}{2}} \times a^{\frac{5}{2}}}{a^{2}}$ in its simplest form.
(b) Express $\frac{2}{\sqrt{3}}$ as a fraction with a rational denominator
(c) Express $\frac{2}{x}+\frac{4}{x+3}, x \neq 0, x \neq-3$, as a single fraction in its simplest form.

## Q77.

Change the subject of the formula $r=\frac{s t}{q}$ tos.

Q74. Water flows through a horizontal pipe of diameter 60 centimetres. The surface width, AB , of the water is 55 centimetres.

(a) Calculate the depth, $d$, of the water in the pipe.
(b) What other depth of water would give the same surface width?

Q76.


The diagram shows part of a football pitch with players at $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D .
BC is perpendicular to $C D$.
$\mathrm{CD}=35$ metres, angle $\mathrm{CDB}=10^{\circ}$, angle $\mathrm{BDA}=10^{\circ}, \mathrm{AD}=34$ metres. Find the distance from A to B .

B10.
Q78.



$$
\begin{aligned}
& \text { The arch of a railway bridge is represented by a parabola. The equation of } \\
& \text { the parabola is } \\
& \qquad y=20-(x-3)^{2} .
\end{aligned}
$$

(a) State the coordinates of the maximum turning point of the parabola. 2
(b) State the equation of the axis of symmetry
(c) Points A and B have the same $y$-coordinate. A is the point $(0,11)$. State the coordinates of $B$.

## National 5 Revision Questions

Q79.

Solve the equation

$$
4 \sin x^{\circ}-1=0, \quad 0 \leq x<360 .
$$

Q80.

In the diagram,
s $P Q$ is the diameter of the circle
s $\mathrm{PQ}=12$ centimetres
s $\mathrm{PR}=10$ centimetres.

Calculate the length of QR .


Give your answer as a surd in its simplest form.
6.
The equation of the parabola in the above diagram is
$y=(x-1)^{2}-16$.
(a) State the coordinates of the minimum turning point of the parabola.
(b) State the equation of the axis of symmetry of the parabola.
(c) The parabola cuts the $x$-axis at A and B . Find the length of AB .

Q82.

State the equation of the axis of symmetry of the parabola
(c) The parabola cuts the $x$-axis at A and B. Find the length of $A B$.


The lines intersect at the point $P$.
Find, algebraically, the coordinates of $P$.
The graph below shows two straight lines
Q81. s $\quad y=2 x-3$
s $x+2 y=14$

Q83.
(a) Evaluate $\left(2^{3}\right)^{2}$.
(b) Hence find $n$, when $\left(2^{3}\right)^{n}=\frac{1}{64}$.

Q84.
A sector of a circle, centre $O$, is shown below.


The radius of the circle is 2.3 metres.
Angle AOB is $65^{\circ}$.
Find the length of the arc $A B$

National 5 Revision Questions

## Q85.

(a) Express $\sqrt{45}-2 \sqrt{5}$ as a surd in its simplest form.
(b) Express as a fraction in its simplest form

$$
\frac{1}{x^{2}}+\frac{1}{x}, \quad x \neq 0 .
$$

Q86.
A necklace is made of beads which are mathematically similar.
$0.8 \mathrm{~cm} \downarrow$


The height of the smaller bead is 0.8 centimetres and its area is 0.6 square centimetres.
The height of the larger bead is 4 centimetres.
Find the area of the larger bead.

Q87.

1. The sketch shows a triangle, ABC .


Calculate the area of the triangle.

Q89 6. A container to hold chocolates is in the shape of part of a cone with dimensions as shown below.


Calculate the volume of the container
Give your answer correct to one significant figure.

Q88.
(a) (i) Factorise completely

$$
3 y^{2}-6 y .
$$

(ii) Factorise

$$
y^{2}+y-6
$$

(b) Hence express $\frac{3 y^{2}-6 y}{y^{2}+y-6}$ in its simplest form.

Q90. ${ }^{\text {(a) Factorise }}$

$$
x^{2}-4 y^{2}
$$

(b) Expand and simplify

$$
(2 x-1)(x+4)
$$

(c) Expand

$$
x^{\frac{1}{2}}\left(3 x+x^{-2}\right)
$$

Q91. The diggam below shows part of the graph of $y=a x^{2}$


Q92.


Write down the values of $a$ and $b$.

The diagram below shows the path of a small rocket which is fired into the marns Q94.

The diagram below shows a circle, centre C .


The radius of the circle is 15 centimetres.
A is the mid-point of chord PQ.
The length of $A B$ is 27 centimetres.
Calculate the length of PQ.
4

Q95. Two grous of people go ta a theatre. Bill buys tickets for 5 adults and 3 children.
The total cost of his tickets is $£ 158 \cdot 25$.
(a) Write down an equation to illustrate this information.
(b) Ben buys tickets for 3 adults and 2 children. The total cost of his tickets is $£ 98$.
Write down an equation to illustrate this information.
(c) Calculate the cost of a ticket for an adult and the cost of a ticket for a child.

Q96.
Lowtown is due west of cidtow
The distance from

- Lowtown to Midtown is 75 kilometres.
- Midtown to Hightown is 110 kilometres
- Hightown to Lowtown is 85 kilometres.


Is Hightown directly north of Lowtown?
Justify your answer.

